CAB301 Assignment 2

Empirical Comparison of Median Calculation Algorithms

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# **Summary**

# **Description of the Algorithm**

The median in statistics is the value that separates the upper half of a set of data, a population, or a probability distribution, from the lower half or simply the middle value within a data set. This value remains extremely important within statistical analysis and probability theory due to the important of what it can represent for a data set or continuous probability distribution. Therefore, it has become of interest to implement a time efficient algorithm that is capable of locating the median value, even in situations where the data set remains unsorted. Thus, an efficient algorithm for locating the median value has been investigated, designed and compared.

## **Brute Force Median**

## **Partitioning Median**

Johnsonbaugh and Schaefer have proposed a version of the median algorithm that is built around the idea that locating the median within an unsorted data set is inherently a sorting problem, or more specifically a selection problem. As the median, as mentioned previously, is the middle value of a discrete data set, we need to only sort the array enough such that we can identify the central value, or the ***kth*** value. This is completed via utilising the underlying principles of the quicksort algorithm, the partitioning of the data set, producing a divide and conquer algorithm.

The implementation of this solution requires three methods, the Median method which handles the unique case of only one element in the data set existing, where it simply returns the value that element. For other data sets, calls the recursive method Select, passing the data set, the indexing value for the first element, the middle value of the data set, and the indexing value for the last element in the data set. This Select method recursively calls itself until the partitioning method returns the desired middle value is returned. It should be noted that upon each call, the algorithm is reduced such that the points of interest lay between ***l*** and ***h***. The work of partially sorting the array is completed by the partitioning method, which is the procedure that is heavily utilised in the Quicksort Algorithm. It first selects a pivot as the first element from the portion of the data set in interest, it then swaps all elements, such that values smaller than the pivot lay on the left-hand side and values greater than the pivot lay on the right-hand side of the pivot. The index value of the pivot is then returned to the selection algorithm for it to be determined if the pivot selected is the median.

# **Theoretical Analysis of the Algorithm**

## **The algorithm’s basic operation**

### **3.1.1 Brute Force Median Algorithm**

### **3.1.2 Partition Median Algorithm**

When conducting the theoretical analysis of the partitioning median algorithm, the basic operation of interest chosen is the comparison of ***A[j] < pivotval*** contained within the partitioning method, as seen in figure …. This statement was selected due to it being a crucial element in not only the partitioning method, but the median algorithm as well. This is due to the fact that the median methods complexity relies on that of the selection method and in turn the partitioning method, with this comparison being the dominant operation. This operation is executed within a ***for*** loop that iterates over an array between the indexes ***l + 1*** and ***h*** as specified by parameters to the partitioning function.

It should be noted that the swapping of elements completed within the partitioning algorithm will have an impact on the execution time. However, during execution of the algorithm, it is believed that this operation will have negligible impact on its order of growth, as it is assumed that the comparison to provide sufficient estimation of the average case efficiency. Thus, the analysis conducted within this report does not consider the swapping of elements operation.

## **Average Case Efficiency**

## **Best Case Efficiency**

## **Worst Case Efficiency**

## **Order of Growth**

# **Methodology, Tools and Techniques**

# **Experimental Results**

## **Functional Testing**

## **Average-Case Number of Basic Operations**

## **Average-Case Execution Time**

# **References**

# **Appendices**

## **Appendix I: Code for Algorithm Implementation**

## **Appendix II: Code for Generating Random Test Data**

## **Appendix III: Code for Testing Functionality**

## **Appendix IV: Code for Basic Operation Count**

## **Appendix V: Code for Time Execution Test**